

28. (a) Free-body diagrams for the blocks  $A$  and  $C$ , considered as a single object, and for the block  $B$  are shown below.  $T$  is the magnitude of the tension force of the rope,  $F_N$  is the magnitude of the normal force of the table on block  $A$ ,  $f$  is the magnitude of the force of friction,  $W_{AC}$  is the combined weight of blocks  $A$  and  $C$  (the magnitude of force  $\vec{F}_{gAC}$  shown in the figure), and  $W_B$  is the weight of block  $B$  (the magnitude of force  $\vec{F}_{gB}$  shown). Assume the blocks are not moving. For the blocks on the table we take the  $x$  axis to be to the right and the  $y$  axis to be upward. From Newton's second law, we have

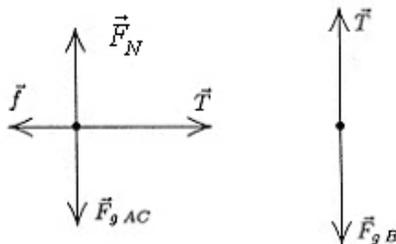
$$x \text{ component: } T - f = 0$$

$$y \text{ component: } F_N - W_{AC} = 0.$$

For block  $B$  take the downward direction to be positive. Then Newton's second law for that block is  $W_B - T = 0$ . The third equation gives  $T = W_B$  and the first gives  $f = T = W_B$ . The second equation gives  $F_N = W_{AC}$ . If sliding is not to occur,  $f$  must be less than  $\mu_s F_N$ , or  $W_B < \mu_s W_{AC}$ . The smallest that  $W_{AC}$  can be with the blocks still at rest is

$$W_{AC} = W_B / \mu_s = (22 \text{ N}) / (0.20) = 110 \text{ N}.$$

Since the weight of block  $A$  is 44 N, the least weight for  $C$  is  $(110 - 44) \text{ N} = 66 \text{ N}$ .



(b) The second law equations become

$$\begin{aligned} T - f &= (W_A/g)a \\ F_N - W_A &= 0 \\ W_B - T &= (W_B/g)a. \end{aligned}$$

In addition,  $f = \mu_k F_N$ . The second equation gives  $F_N = W_A$ , so  $f = \mu_k W_A$ . The third gives  $T = W_B - (W_B/g)a$ . Substituting these two expressions into the first equation, we obtain

$$W_B - (W_B/g)a - \mu_k W_A = (W_A/g)a.$$

Therefore,

$$a = \frac{g(W_B - \mu_k W_A)}{W_A + W_B} = \frac{(9.8 \text{ m/s}^2)(22 \text{ N} - (0.15)(44 \text{ N}))}{44 \text{ N} + 22 \text{ N}} = 2.3 \text{ m/s}^2.$$