

32. We adopt the positive direction choices used in the textbook so that equations such as Eq. 4-22 are directly applicable. The initial velocity is horizontal so that  $v_{0,y} = 0$  and  $v_{0,x} = v_0 = 161 \text{ km/h}$ . Converting to SI units, this is  $v_0 = 44.7 \text{ m/s}$ .

(a) With the origin at the initial point (where the ball leaves the pitcher's hand), the  $y$  coordinate of the ball is given by  $y = -\frac{1}{2}gt^2$ , and the  $x$  coordinate is given by  $x = v_0t$ . From the latter equation, we have a simple proportionality between horizontal distance and time, which means the time to travel half the total distance is half the total time. Specifically, if  $x = 18.3/2 \text{ m}$ , then  $t = (18.3/2)/44.7 = 0.205 \text{ s}$ .

(b) And the time to travel the next  $18.3/2 \text{ m}$  must also be  $0.205 \text{ s}$ . It can be useful to write the horizontal equation as  $\Delta x = v_0\Delta t$  in order that this result can be seen more clearly.

(c) From  $y = -\frac{1}{2}gt^2$ , we see that the ball has reached the height of  $|\frac{1}{2}(9.80)(0.205)^2| = 0.205 \text{ m}$  at the moment the ball is halfway to the batter.

(d) The ball's height when it reaches the batter is  $-\frac{1}{2}(9.80)(0.409)^2 = -0.820 \text{ m}$ , which, when subtracted from the previous result, implies it has fallen another  $0.615 \text{ m}$ . Since the value of  $y$  is not simply proportional to  $t$ , we do not expect equal time-intervals to correspond to equal height-changes; in a physical sense, this is due to the fact that the initial  $y$ -velocity for the first half of the motion is not the same as the "initial"  $y$ -velocity for the second half of the motion.