

13. (a) The free-body diagram for the crate is shown below. \vec{T} is the tension force of the rope on the crate, \vec{F}_N is the normal force of the floor on the crate, $m\vec{g}$ is the force of gravity, and \vec{f} is the force of friction. We take the $+x$ direction to be horizontal to the right and the $+y$ direction to be up. We assume the crate is motionless. The equations for the x and the y components of the force according to Newton's second law are:

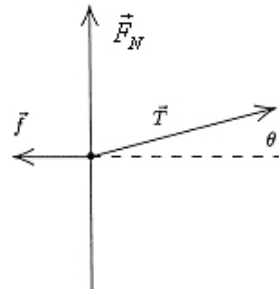
$$\begin{aligned}T \cos \theta - f &= 0 \\T \sin \theta + F_N - mg &= 0\end{aligned}$$

where $\theta = 15^\circ$ is the angle between the rope and the horizontal. The first equation gives $f = T \cos \theta$ and the second gives $F_N = mg - T \sin \theta$. If the crate is to remain at rest, f must be less than $\mu_s F_N$, or $T \cos \theta < \mu_s (mg - T \sin \theta)$. When the tension force is sufficient to just start the crate moving, we must have

$$T \cos \theta = \mu_s (mg - T \sin \theta).$$

We solve for the tension:

$$\begin{aligned}T &= \frac{\mu_s mg}{\cos \theta + \mu_s \sin \theta} \\&= \frac{(0.50)(68)(9.8)}{\cos 15^\circ + 0.50 \sin 15^\circ} \\&= 304 \approx 3.0 \times 10^2 \text{ N}.\end{aligned}$$



(b) The second law equations for the moving crate are

$$\begin{aligned}T \cos \theta - f &= ma \\F_N + T \sin \theta - mg &= 0.\end{aligned}$$

Now $f = \mu_k F_N$, and the second equation gives $F_N = mg - T \sin \theta$, which yields $f = \mu_k (mg - T \sin \theta)$. This expression is substituted for f in the first equation to obtain

$$T \cos \theta - \mu_k (mg - T \sin \theta) = ma,$$

so the acceleration is

$$a = \frac{T (\cos \theta + \mu_k \sin \theta)}{m} - \mu_k g.$$

Numerically, it is given by

$$a = \frac{(304 \text{ N})(\cos 15^\circ + 0.35 \sin 15^\circ)}{68 \text{ kg}} - (0.35)(9.8 \text{ m/s}^2) = 1.3 \text{ m/s}^2.$$