

56. The height reached by the player is  $y = 0.76$  m (where we have taken the origin of the  $y$  axis at the floor and  $+y$  to be upward).

(a) The initial velocity  $v_0$  of the player is

$$v_0 = \sqrt{2gy} = \sqrt{2(9.8)(0.76)} = 3.86 \text{ m/s}.$$

This is a consequence of Eq. 2-16 where velocity  $v$  vanishes. As the player reaches  $y_1 = 0.76 - 0.15 = 0.61$  m, his speed  $v_1$  satisfies  $v_0^2 - v_1^2 = 2gy_1$ , which yields

$$v_1 = \sqrt{v_0^2 - 2gy_1} = \sqrt{(3.86)^2 - 2(9.80)(0.61)} = 1.71 \text{ m/s}.$$

The time  $t_1$  that the player spends *ascending* in the top  $\Delta y_1 = 0.15$  m of the jump can now be found from Eq. 2-17:

$$\Delta y_1 = \frac{1}{2} (v_1 + v) t_1 \Rightarrow t_1 = \frac{2(0.15)}{1.71 + 0} = 0.175 \text{ s}$$

which means that the total time spent in that top 15 cm (both ascending and descending) is  $2(0.17) = 0.35 \text{ s} = 350 \text{ ms}$ .

(b) The time  $t_2$  when the player reaches a height of 0.15 m is found from Eq. 2-15:

$$0.15 = v_0 t_2 - \frac{1}{2} g t_2^2 = (3.86) t_2 - \frac{9.8}{2} t_2^2,$$

which yields (using the quadratic formula, taking the smaller of the two positive roots)  $t_2 = 0.041 \text{ s} = 41 \text{ ms}$ , which implies that the total time spent in that bottom 15 cm (both ascending and descending) is  $2(41) = 82 \text{ ms}$ .