

Precision Polarimetry at JLab, 6 GeV Era

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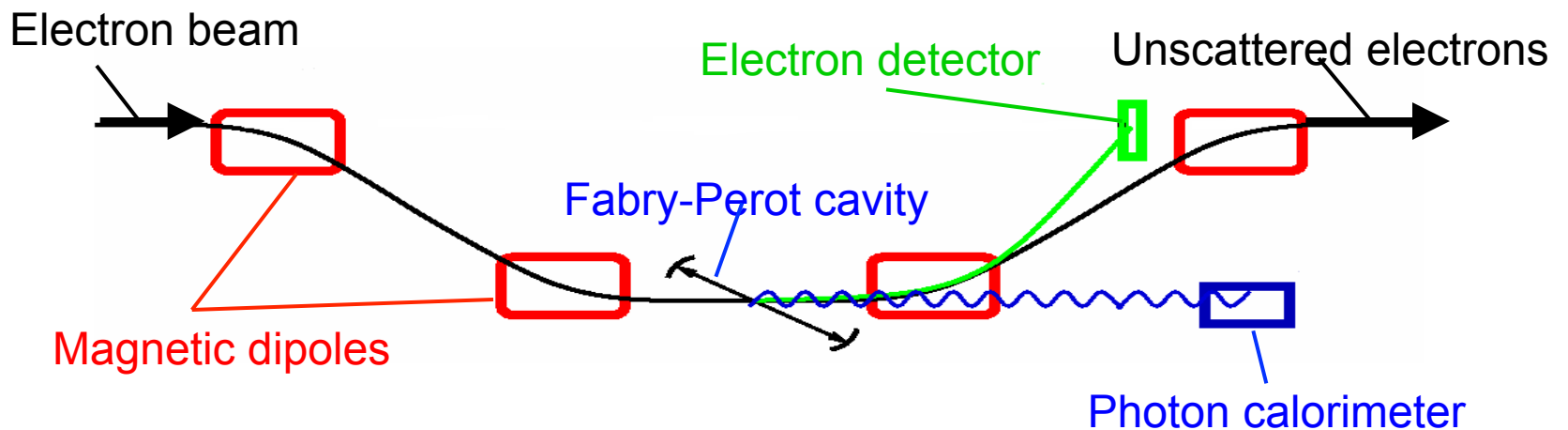
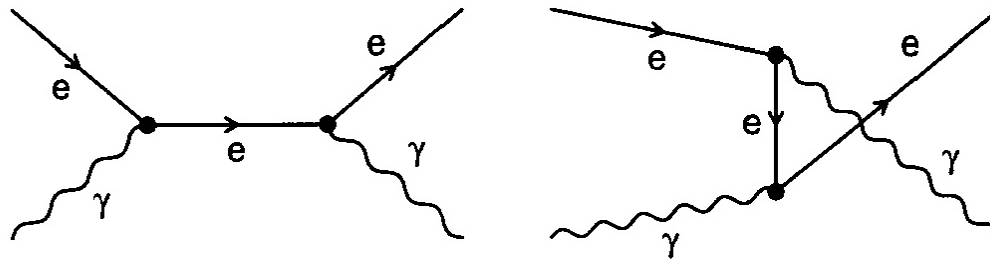
Hall A Compton Upgrade Team: M. Friend, D. Parno, F. Benmokhtar, A. Camsonne, G.B. Franklin, R. Michaels, S. Nanda, K. Paschke, B. Quinn, P. Souder

- Compton Scattering as a Polarimetry Tool
 - General Considerations
 - Complications and Systematic Errors
- JLab Hall A Compton Photon Calorimeter
 - GSO Performance (Simulations and benchmarks)
 - Integrating DAQ
- Polarimeter Performance Results

Compton Polarimetry

Electron beam passes through polarized photon beam

Spin-dependence of Compton scattering $\rightarrow$ analyzing power



Unpolarized Cross Section

Very forward peaked (GeV electrons on eV photons)

Example:

Beam

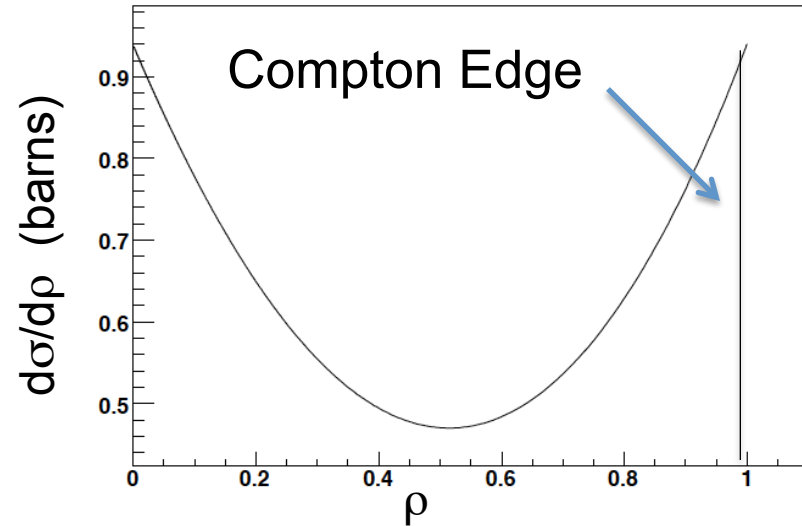
$$E = 3.48 \text{ GeV}$$

Cavity Photons

$$\omega_0 = 1.165 \text{ eV}$$

Compton Edge

$$\omega_{\max} = 204 \text{ MeV}$$



Max photon energy

$$\rho \equiv \omega / \omega_{\max}$$

$$\omega_{\max} = 4 \frac{E^2 \omega_0}{m_e^2 c^4} a$$

$$a \equiv 1 / \left(1 + \frac{4\omega_0 E}{m_e^2 c^4} \right)$$

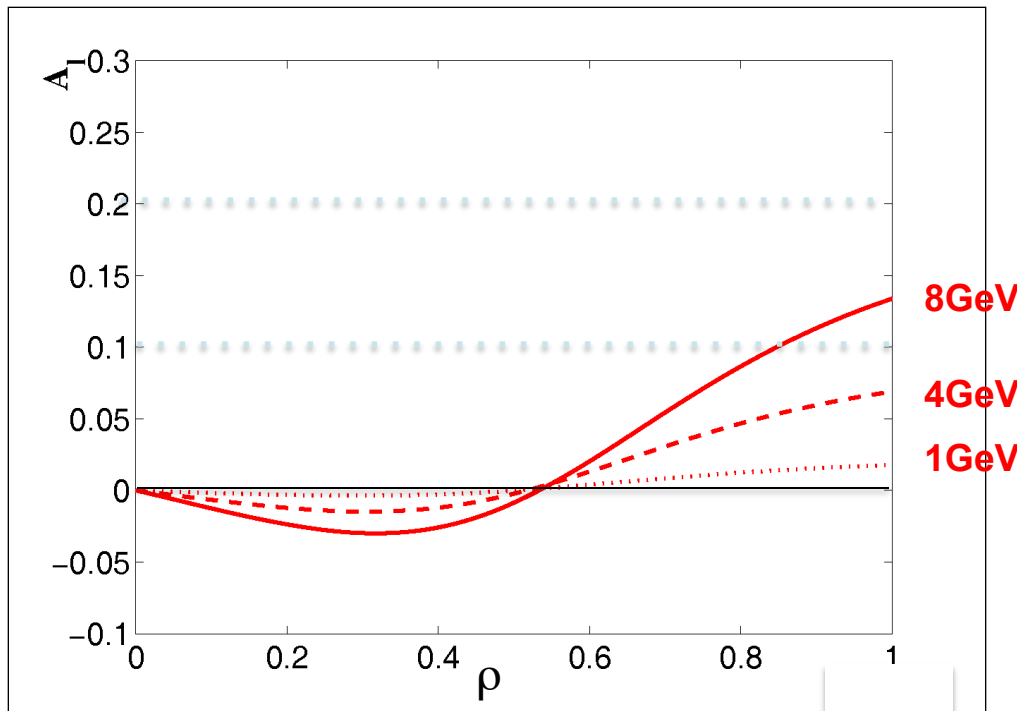
Klein-Nishina Formula

$$\left(\frac{d\sigma}{d\rho} \right)_{\text{unpol}} = 2\pi r_0^2 a \left[\frac{\rho^2 (1-a)^2}{1 - \rho(1-a)} + 1 + \left(\frac{1 - \rho(1+a)}{1 - \rho(1-a)} \right)^2 \right]$$

Compton Analyzing Power

$$A_l(\rho) \equiv \frac{\sigma^{\uparrow\uparrow} - \sigma^{\uparrow\downarrow}}{\sigma^{\uparrow\uparrow} + \sigma^{\uparrow\downarrow}} = \frac{2\pi r_0^2}{d\sigma/d\rho} a(1 - \rho(1 + a)) \left[1 - \frac{1}{(1 - \rho(1 - a))^2} \right]$$

- Peak analyzing power 1% to 20%
- Strong dependence on scattered photon energy

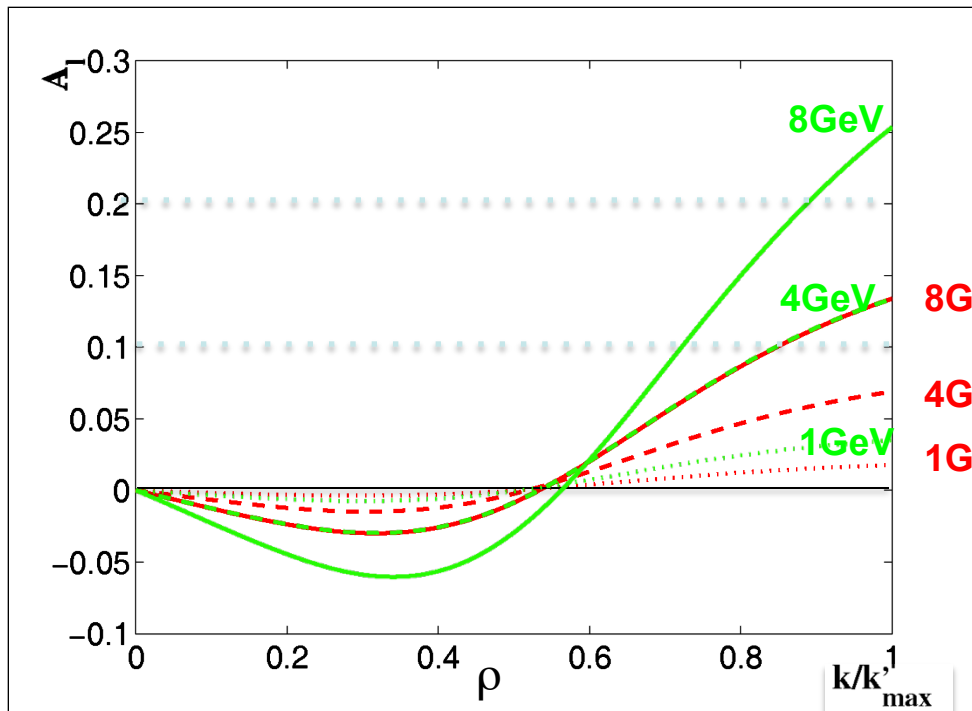


$\lambda=1064\text{nm}$, $\omega_0=1.165\text{ eV}$

Compton Analyzing Power

$$A_l(\rho) \equiv \frac{\sigma^{\uparrow\uparrow} - \sigma^{\uparrow\downarrow}}{\sigma^{\uparrow\uparrow} + \sigma^{\uparrow\downarrow}} = \frac{2\pi r_0^2}{d\sigma/d\rho} a(1 - \rho(1 + a)) \left[1 - \frac{1}{(1 - \rho(1 - a))^2} \right]$$

- Peak analyzing power 1% to 20%
- Strong dependence on scattered photon energy



$\lambda=1064\text{nm}$, $\omega_0=1.165\text{ eV}$

$\lambda=532\text{nm}$, $\omega_0=2.330\text{ eV}$

Doubling laser $\rightarrow$
energy doubles analyzing power

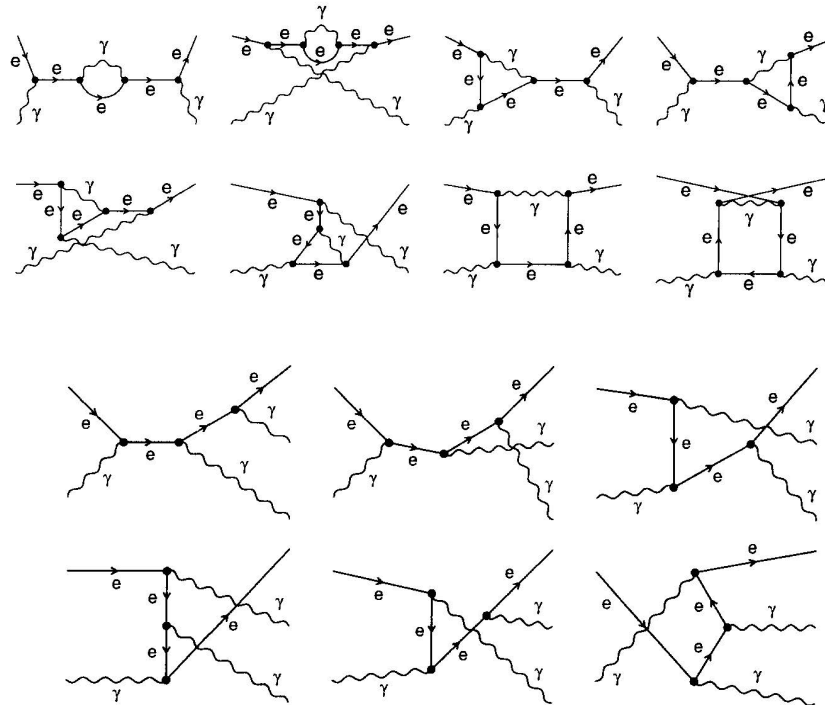
Negligible theoretical error

Higher order diagrams

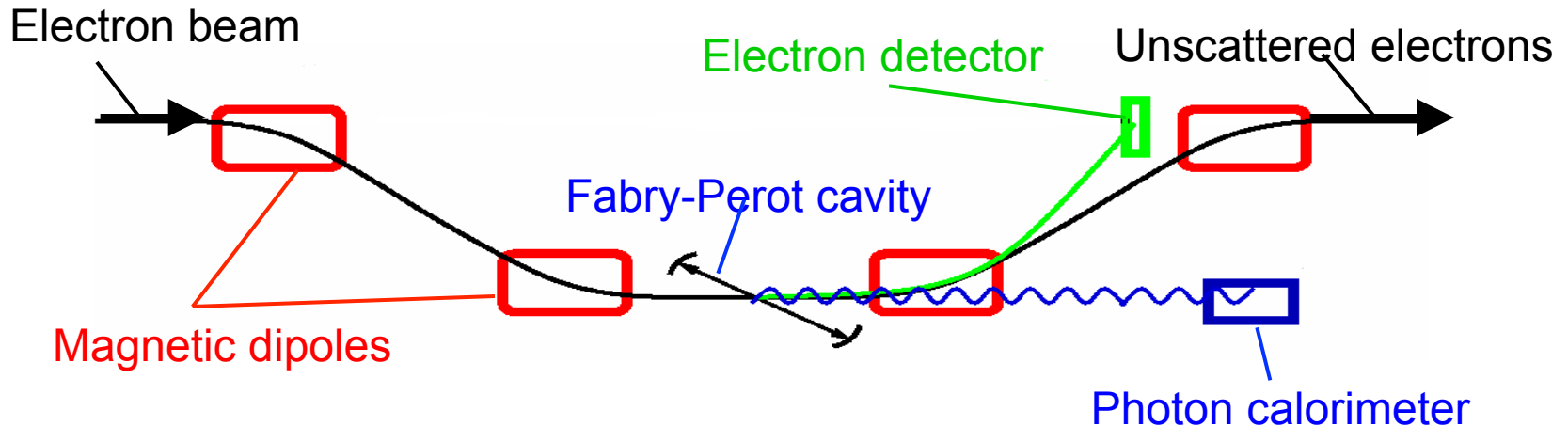
Denner & Dittmaier Nucl. Phys. B540 (1999)

$\sim 0.3\%$ correction to A_1 at 3.5 GeV beam energy

Increases with energy



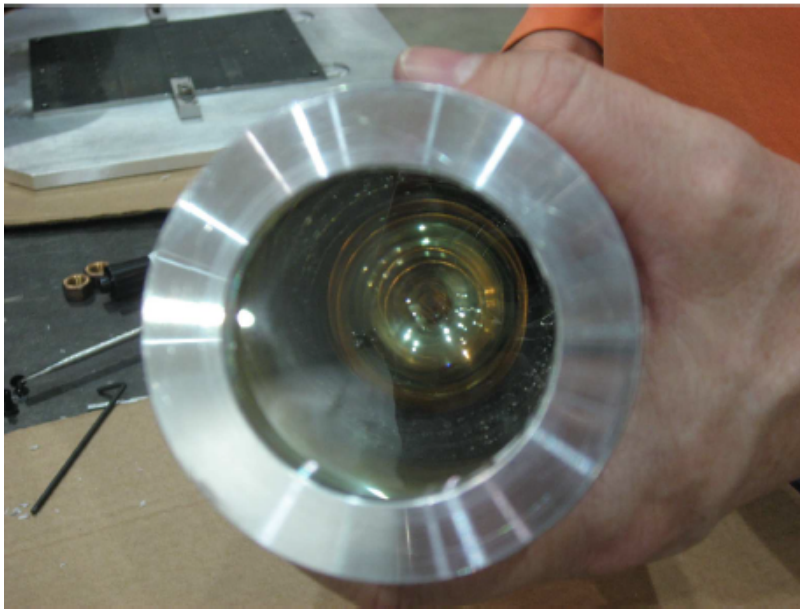
Experimental Challenges



- Thresholds and non-linearities a problem
(Strong energy dependence of A_1)
- Large dynamic range of photon energies
(Compton edge varies from ~ 20 MeV to ~ 500 MeV)
- Electrons or photons can be detected
 - Scattered electrons near beam halo at low beam energies
 - Photon detection requires knowledge of resolution function

Hall A Compton Photon Calorimeter

- Single GSO crystal manufactured by Hitachi Chemical
0.5% Ce-doped Gd_2SiO_5
6 cm diam x 15 cm length
- Flash ADC integrates Compton signal
Customized Struck SIS3320 FADC
No threshold, Dead-timeless
1 Primary Data word for each 1/30 sec helicity period
Auxiliary monitoring info



• Crystal Properties

	GSO	PbWO ₄	BGO	CeF ₃	BriLanCe 380	PreLude 420
Density (g/cm ³)	6.70	8.30	7.13	6.16	5.29	7.1
Rad Length (cm)	1.39	0.90	1.12	1.68	~1.9	1.2
Moliere Radius (cm)	2.4	2.0	2.3	2.6	?	?
Decay time (ns)	~80	50	300	30	16	41
Light output (% NaI)	45%	0.4%	9%	6.6%	165%	84%
photoelectrons (# / MeV)	850	8	170	125	3150	1600

Energy Weighted Asymmetry:

$$E^{\pm} = LT \int_0^{E_{\max}} \varepsilon(E) E \frac{d\sigma}{dE}(E) (1 \pm P_e P_{\gamma} A_l(E)) dE$$

$$A_{Exp} = \frac{E^{+} - E^{-}}{E^{+} + E^{-}}$$

Longitudinal Compton Asymmetry

Actual Asymmetry Weighted by Detector Signal

$$S^{\pm} = LT \int_0^{E_{\max}} s(E) \frac{d\sigma}{dE}(E) (1 \pm P_e P_{\gamma} A_l(E)) dE$$

Average detector signal for photon energy E

$$A_{Exp} = \frac{S^{+} - S^{-}}{S^{+} + S^{-}} = P_e P_{\gamma} \frac{\int_0^{E_{\max}} A_l(E) s(E) \frac{d\sigma}{dE}(E) dE}{\int_0^{E_{\max}} s(E) \frac{d\sigma}{dE}(E) dE} = P_e P_{\gamma} A_{lS}$$

Energy Weighted Asymmetry:

$$E^{\pm} = LT \int_0^{E_{\max}} \varepsilon(E) E \frac{d\sigma}{dE}(E) dE$$

$$A_{Exp} = \frac{E^{+} - E^{-}}{E^{+} + E^{-}}$$

average response
function required

Actual Asymmetry Weighted by Detector Response

$$S^{\pm} = LT \int_0^{E_{\max}} s(E) \frac{d\sigma}{dE}(E) (1 \pm P_e P_{\gamma} A_l(E)) dE$$

Average detector signal for photon energy E

$$A_{Exp} = \frac{S^{+} - S^{-}}{S^{+} + S^{-}} = P_e P_{\gamma} \frac{\int_0^{E_{\max}} A_l(E) s(E) \frac{d\sigma}{dE}(E) dE}{\int_0^{E_{\max}} s(E) \frac{d\sigma}{dE}(E) dE} = P_e P_{\gamma} A_{ls}$$

Statistical Considerations

$$P_e = \frac{1}{P_\gamma} \frac{1}{A_{ls}} A_{exp}$$

Goal: 0.01

Photon polarization ~1

Analyzing Power ~1/.02 (worst case)

Error on Integrated Signal Need <.0002

$$\sigma_{P_e} = \frac{1}{P_\gamma} \frac{1}{A_{ls}} \frac{\sigma_s}{s}$$

Energy Weighted Statistics

$$\left[\frac{\sigma_s}{s} \right]^2 = \frac{\int_0^{E_m} dE E^2 \frac{dN}{dE}}{\left[\int_0^{E_m} dE E \frac{dN}{dE} \right]^2} = \frac{\int_0^{1_m} d\rho \rho^2 \frac{dN}{d\rho}}{\left[\int_0^{1_m} d\rho \rho \frac{dN}{d\rho} \right]^2}$$

$$\frac{\sigma_s}{s} = 1.2 \frac{1}{\sqrt{N}} \quad (\text{Using Compton shape for } dN/d\rho)$$

100 kHz counting rate → Statistical accuracy in a few hours

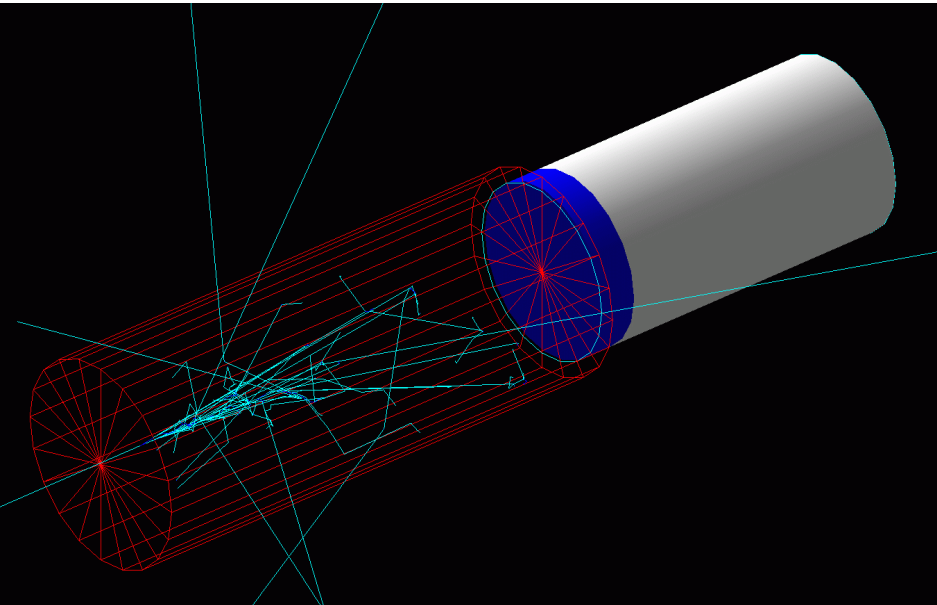
Systematic Considerations Dominate

$$S^{\pm} = LT \int_0^{E_{\max}} s(E) \frac{d\sigma}{dE}(E) (1 \pm P_e P_{\gamma} A_l(E)) dE$$

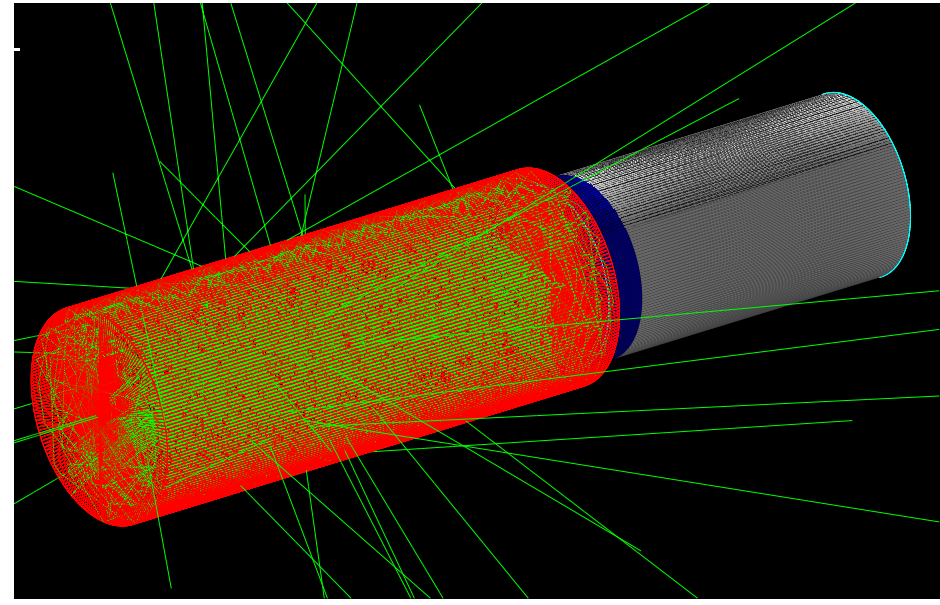
Function of detector and electronics response

Detector Response: GEANT4 Simulations Performed

Vahe Mamyán & Megan Friend



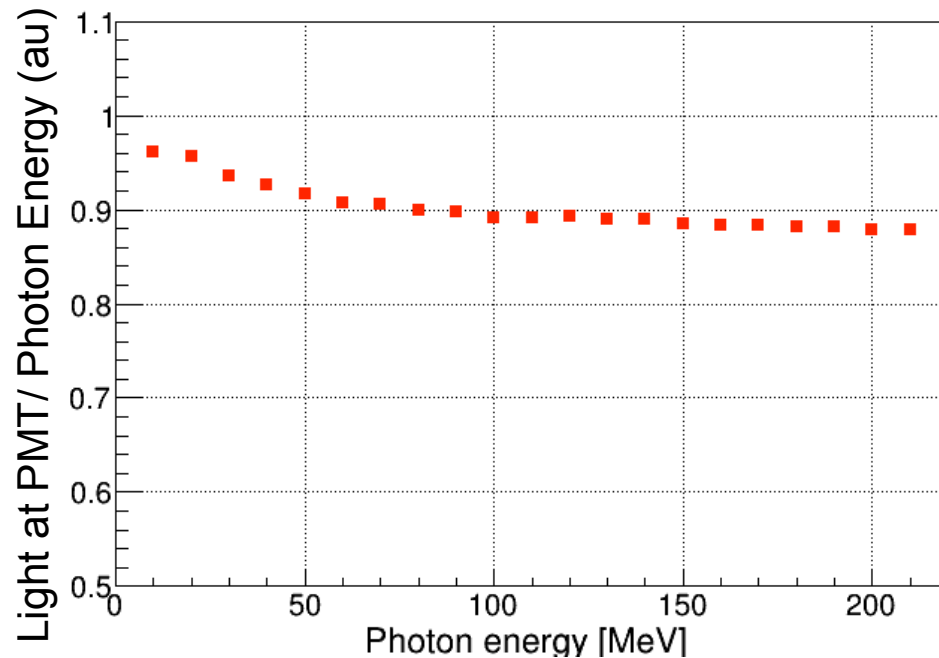
Shower Generation
200 MeV Photon Event



Optical Photon Tracking
30 MeV Photon Event

GEANT produces GSO average response, $s(E)$

$$A_{ls} =_{\gamma} \frac{\int_0^{E_{\max}} A_l(E) s(E) \frac{d\sigma}{dE}(E) dE}{\int_0^{E_{\max}} s(E) \frac{d\sigma}{dE}(E) dE}$$



Verification of Detector Response Simulations

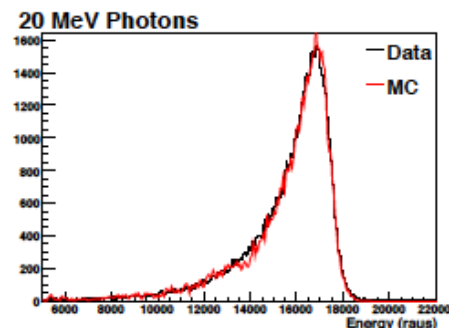
Tests at Duke's HIGS facility

“Monoenergetic” photons

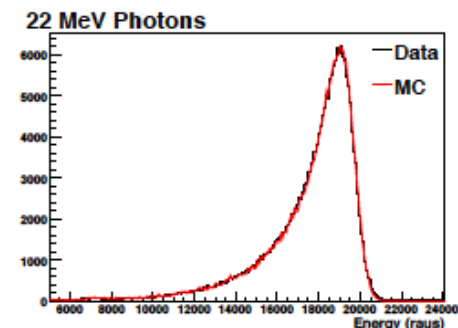
20, 22, 25, 30, & 40 MeV

See D. Parno et. al.

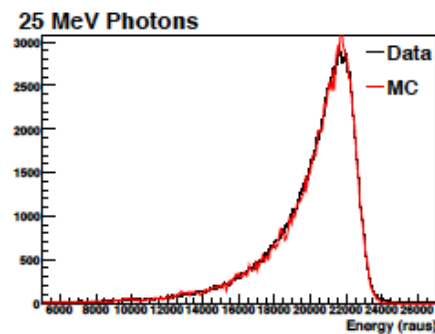
NIM A (2013) DOI 10.1016



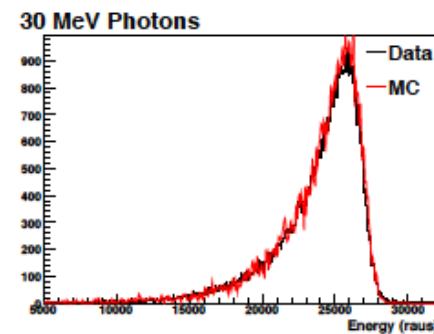
(a)



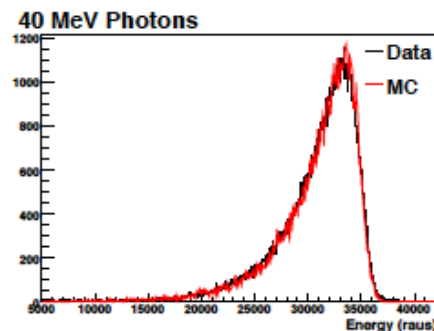
(b)



(c)



(d)

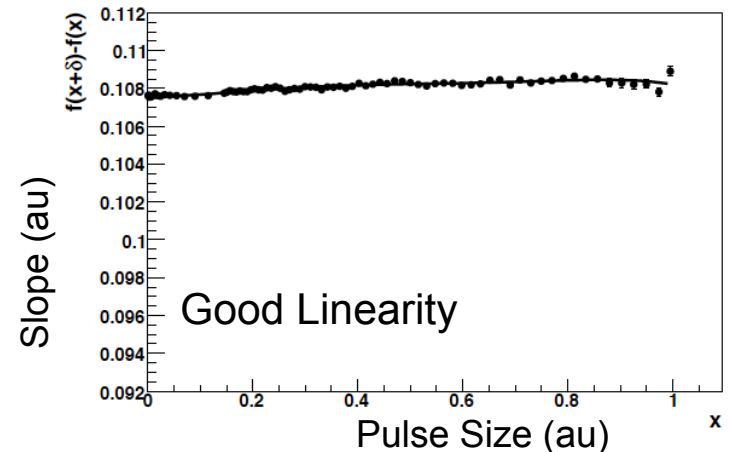
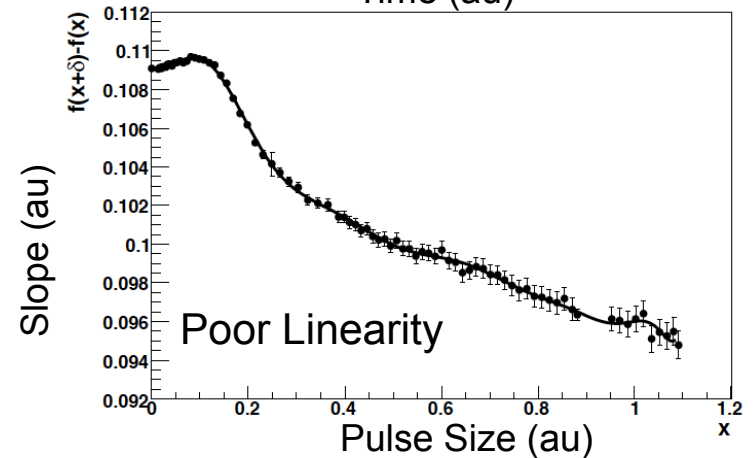
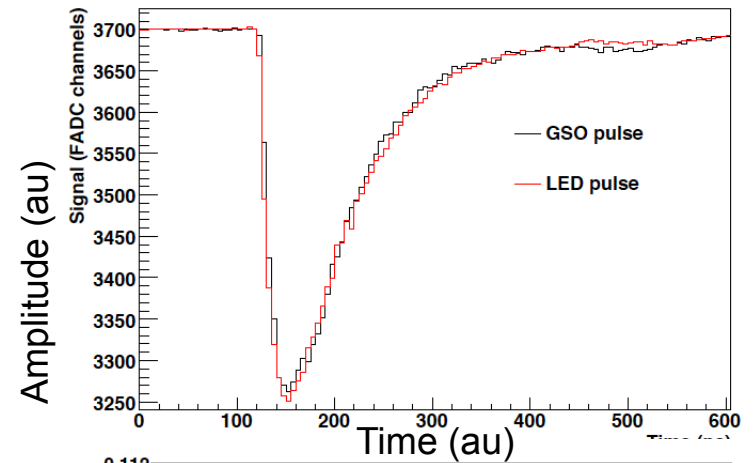


(e)

Systematic Considerations

PMT Linearity

Mapped with 2-LED Pulser System
Simulated GSO pulse
Measures PMT/Base linearity
Monitors gain shifts



Systematic Considerations

Time-Dependent Systematics & Background

Electron Beam Helicity Flipped at ~ 30 Hz (pseudo-random)

Fabry-Perot Cavity Laser Cycle:

- 60 sec Locked on Right Circular Polarization

- 30 sec Unlocked (used for background subtraction)

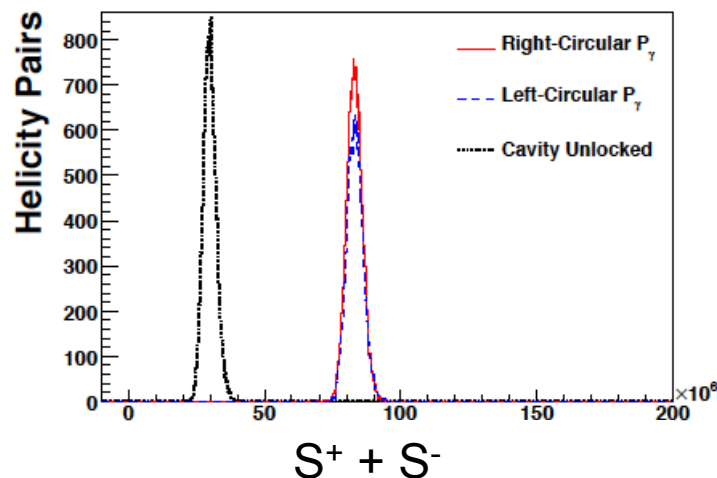
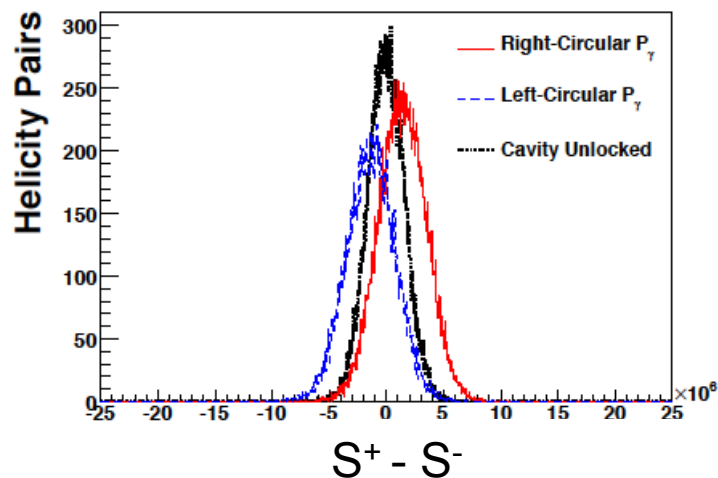
- 60 sec Locked on Left Circular Polarization

- 30 sec Unlocked

Significant background

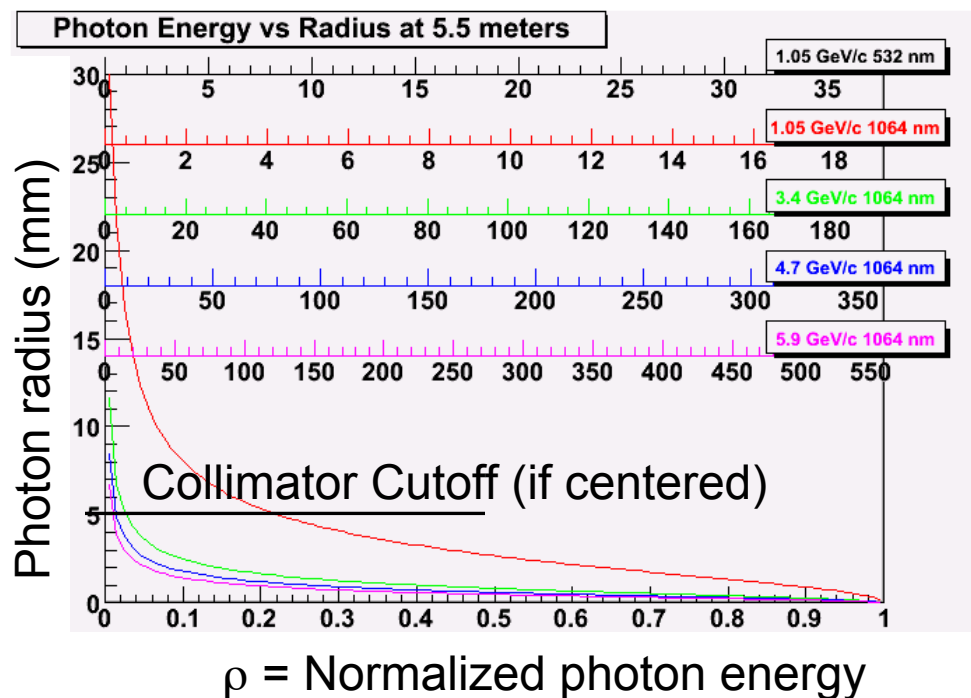
Synchrotron Radiation and Beam-Halo Bremsstrahlung

Synchrotron Radiation $\sim E^4$... potential problem for 12 GeV running

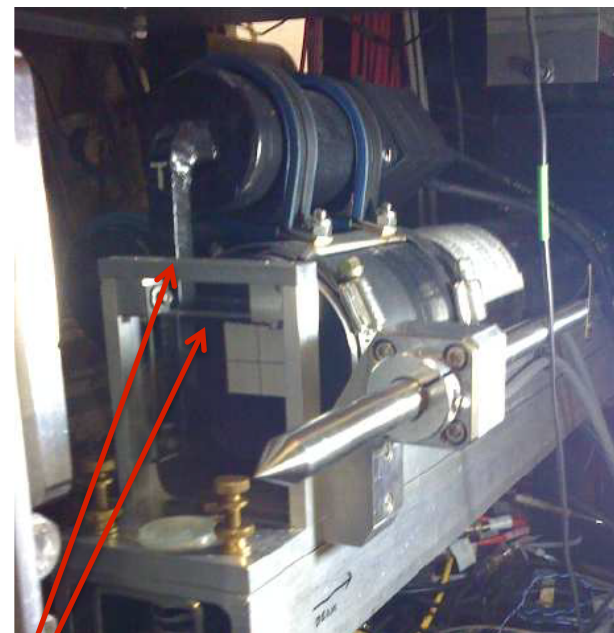


Systematic Considerations

Geometry and Alignment



If misaligned, collimators can distort energy spectrum at low end



1mm tungsten radiators/ scintillators
Used for horizontal and vertical scans

Systematic Considerations

Verification

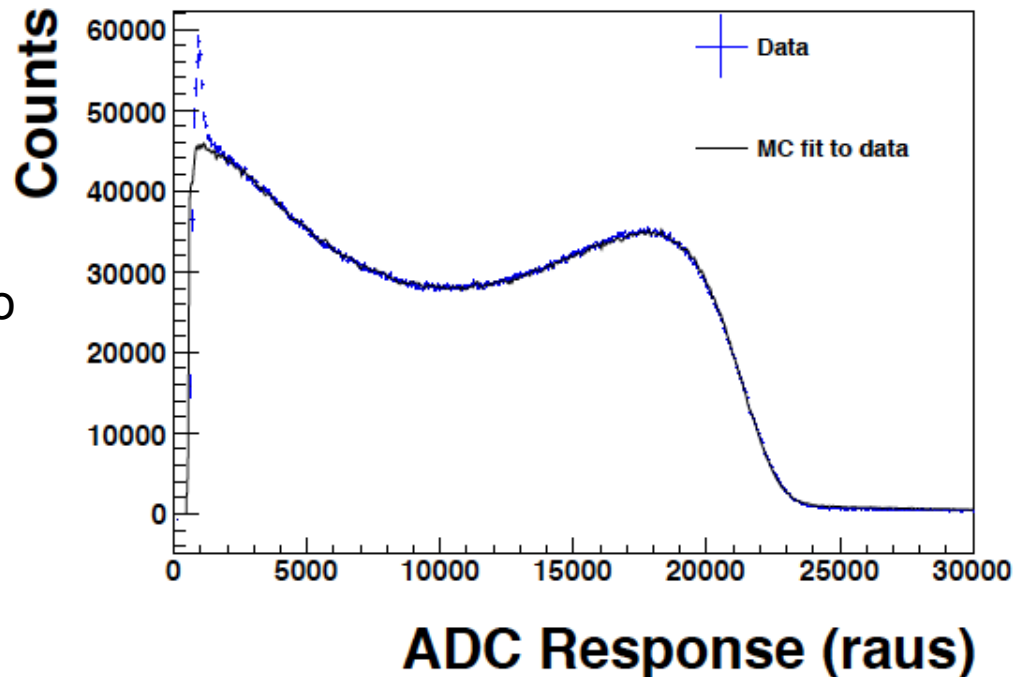
For each helicity period, FADC Data-stream includes:

- Signal Sum (Main analysis)

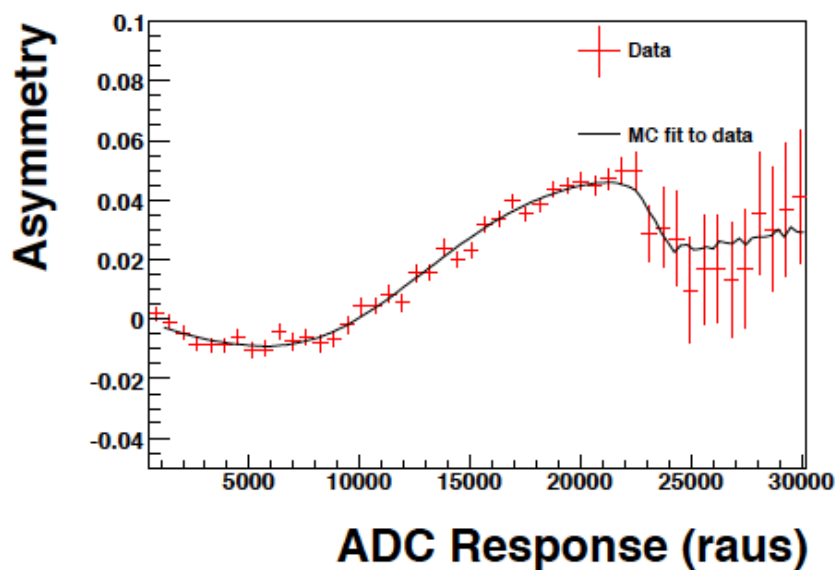
- Prescaled Integrated Triggered GSO Pulses

- Random Sampled FADC sample periods

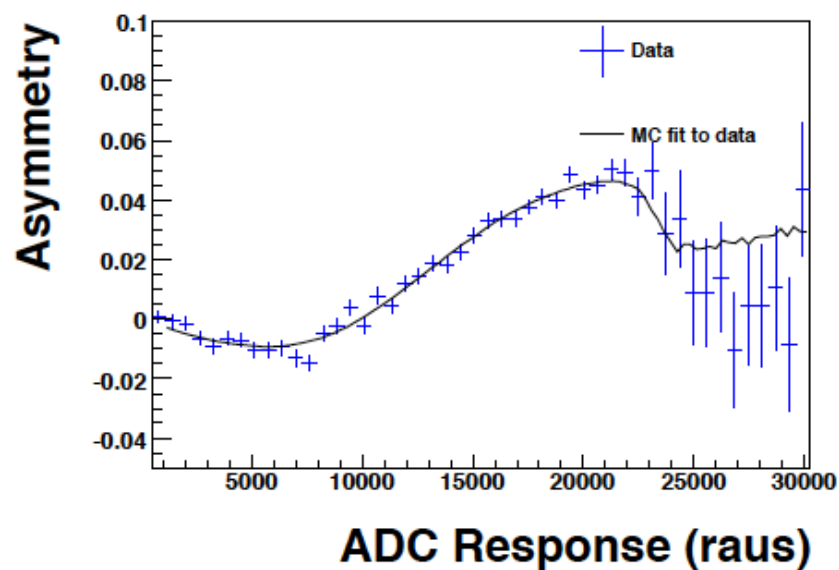
Triggered Compton GSO data
Data compared to Monte Carlo



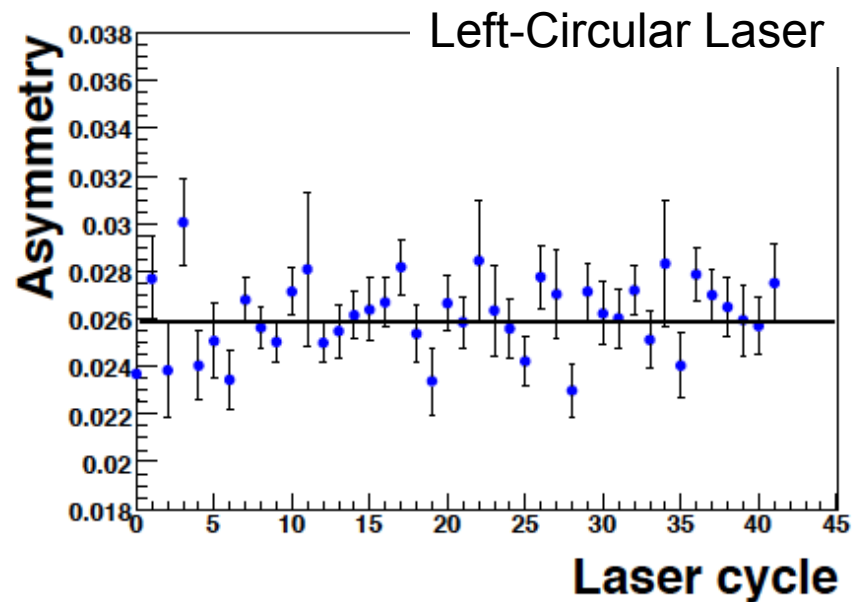
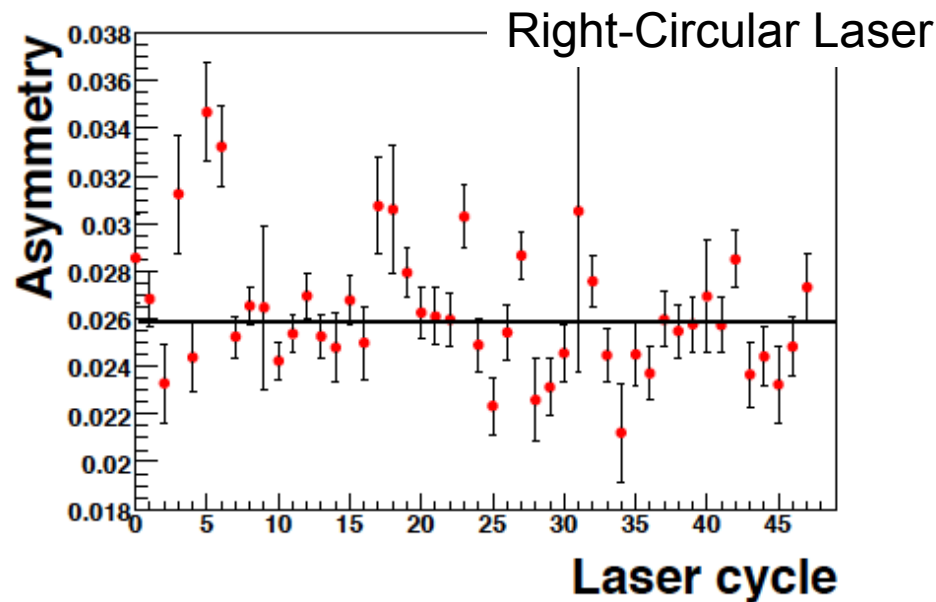
Prescaled triggered data can be used to measure polarization



(a)



(b)



(a)

(b)

Figure 4.25: A typical Compton slug for (a) laser-right and (b) laser-left, where the asymmetry is positive after being scaled as in Eq. 4.58. Each data point is a separate laser-cycle including local background subtraction. Error bars are statistical as defined in Sec. 4.5.3.1, and the solid line is a constant fit to the data. Plots of all of the Compton slugs, as well as a table of the measured asymmetry and statistical error for each slug, are given in Appendix A.

From: M. Friend et al., Upgraded photon calorimeter...

Systematic Errors	
Laser Polarization	0.80%
Signal Analyzing Power:	
Nonlinearity	0.30%
Energy Uncertainty	0.10%
Collimator Position	0.05%
Analyzing Power Total Uncertainty	0.33%
Gain Shift:	
Background Uncertainty	0.31%
Pedestal on Gain Shift	0.20%
Gain Shift Total Uncertainty	0.37%
Total Uncertainty	0.94%

Conclusion

- Accuracy of 1% has been achieved
- Significant improvements possible
 - Improved determination of photon polarization
 - Reduction in Synchrotron Radiation
(Particularly for high electron beam energy)
 - Careful monitoring of gain shifts
(Cavity on vs. Cavity off)

Example Compton Edge and Analyzing Powers

E_e (MeV)	$\omega_0 = 1.165 \text{ eV (IR)}$			$\omega_0 = 2.33 \text{ eV (green)}$		
	a	ω_{max} (MeV)	A_{max}	a	ω_{max} (MeV)	A_{max}
1,375	.976	33	.024	.953	64	.048
2,750	.953	129	.047	.911	246	.093
5,500	.911	492	.093	.836	903	.177
11,000	.817	1,806	.177	.718	3,101	.320